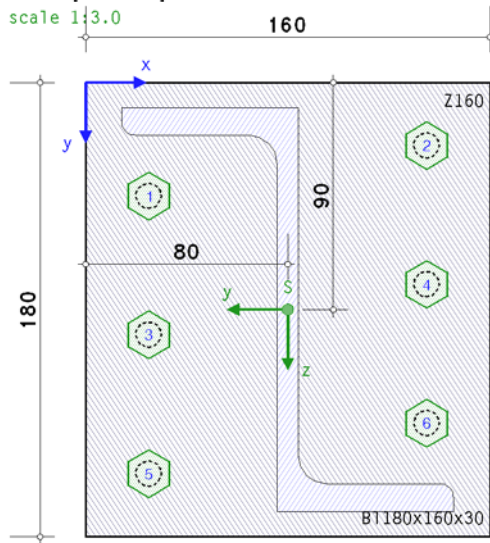


POS. 4: Z-SECTION

bolted end-plate connection EC 3-1-8 (12.10), NA: Deutschland

4H-EC3FS version: 2/2025-1b

1. input report



steel grade

steel grade S355

bolts

bolt class 8.8, bolt size M10, normal wrench size

thread included in the shear plane

connection

end-plate (rectangular): thickness $t_p = 30.0$ mm, width $b_p = 160.0$ mm, length $l_p = 180.0$ mm

beam: section Z160

beam-end-plate: surrounding fillet weld, weld thickness $a = 10.0$ mm

beam section centric on end-plate (beam centroid in plate centre)

coordinates of the beam centroid on end-plate $x_s = 80.0$ mm, $y_s = 90.0$ mm

bolts:

coordinates of bolt axis:

$x_1 = 25.0$ mm, $y_1 = 45.0$ mm

$x_2 = 135.0$ mm, $y_2 = 25.0$ mm

$x_3 = 25.0$ mm, $y_3 = 100.0$ mm

$x_4 = 135.0$ mm, $y_4 = 80.0$ mm

$x_5 = 25.0$ mm, $y_5 = 155.0$ mm

$x_6 = 135.0$ mm, $y_6 = 135.0$ mm

calculation

verification:

calculation of internal forces and moments (FEM) and verifications of resistance

verification of end-plate with the plastic method, verification of compression by contact

verification of beam section with the plastic method

verification of welds with the directional method

verification of bolts, check of distances

FEM-calculation:

bolts are plastically calculated, spring constant of bolts $c_f = 1741.2$ kN/cm

plastic limit force $F_{t,f} = f_{t,f} \cdot F_{t,Rd} = 31.7$ kN, $f_{t,f} = 0.950$, $F_{t,Rd} = (k_2 \cdot f_{ub} \cdot A_s) / \gamma_{M2} = 33.41$ kN, $k_2 = 0.90$

effective elongation at failure $\epsilon_{t,f} = f_{t,e} \cdot \epsilon_{ub} = 3.0\%$, $f_{t,e} = 0.250$, $\epsilon_{ub} = 12.0\%$

without preloading ($F_{p,c} = 0$)

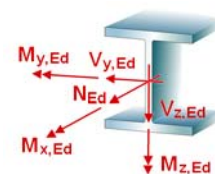
effective foundation modulus of end plate $c_b = 7000.0$ kN/cm³

number / dimension of finite elements each direction $n_x / \Delta x = 26 / 6.2$ mm, $n_y / \Delta y = 30 / 6.0$ mm

max. 50 iteration steps (tolerance limit 5‰)

internal forces and moments referring to local axes of cross-section

Lk	N_{Ed} kN	$M_{y,Ed}$ kNm	$V_{z,Ed}$ kN	$M_{z,Ed}$ kNm	$V_{y,Ed}$ kN	$M_{x,Ed}$ kNm
1	-9.61	-0.50	0.78	2.58	1.37	0.80
2	8.45	2.97	23.13	10.43	5.10	0.05
3	-3.69	0.01	0.58	-5.59	-2.87	0.78
4	2.96	2.77	23.19	12.14	6.00	0.05
5	-8.86	-0.02	0.69	3.28	1.68	0.01
6	5.44	2.39	23.19	6.24	3.00	1.17
7	-2.93	0.49	0.49	-4.90	-2.55	-0.01
8	1.88	2.08	23.32	11.15	5.55	1.18
9	-3.92	1.30	16.64	9.57	4.80	0.83
10	-3.17	1.78	16.55	10.26	5.12	0.04



partial safety factors for material

resistance of cross-sections $\gamma_{M0} = 1.00$

resistance of bolts, welds, plates in bearing $\gamma_{M2} = 1.25$

local stresses especially of the beam and of welds are not considered !

utilizations

in utilization of bolts due to tension $U_{t,s}$ ist minimum plastic utilization of the connection U_{pl} and plastic utilization of tensile forces of bolts $U_{pl,t,s}$ is included.

Lk	U_p	U_σ	U_b	$U_{pl,s}$	$U_{pl,t,s}$	$U_{wt,s}$	$U_{t,s}$	$U_{vt,s}$	$U_{b,s}$	U_q	$U_{c/t}$	U_w	U
1	0.146	0.146	0.097	0.125	0.136	0.023	0.018	0.237	0.010	0.389	0.460	0.204	0.460
2	0.537	0.537	0.396	0.767	0.663	0.224	0.082	0.711	0.035	0.695	0.479	0.747	0.767
3	0.309	0.309	0.205	0.366	0.327	0.061	0.050	0.463	0.011	0.529	0.462	0.419	0.529
4	0.657	0.657	0.490	0.856	0.746	0.294	0.082	0.741	0.046	0.820	0.476	0.874	0.874
5	0.181	0.181	0.121	0.177	0.179	0.032	0.026	0.227	0.002	0.235	0.469	0.250	0.469
6	0.289	0.289	0.216	0.462	0.414	0.091	0.074	0.626	0.030	0.648	0.487	0.440	0.648
7	0.276	0.276	0.178	0.322	0.291	0.052	0.042	0.359	0.002	0.355	0.455	0.372	0.455
8	0.607	0.607	0.420	0.781	0.708	0.199	0.082	0.690	0.034	0.916	0.473	0.807	0.916*
9	0.520	0.520	0.350	0.640	0.594	0.128	0.082	0.685	0.023	0.749	0.471	0.700	0.749
10	0.558	0.558	0.378	0.692	0.649	0.155	0.082	0.698	0.024	0.701	0.474	0.746	0.746

U_p : utilization of end-plate; U_σ : utilization of end-plate due to stress; U_b : utilization of end-plate due to compression by contact

$U_{pl,s}$: minimum plastic utilization of the connection; $U_{pl,t,s}$: plastic utilization of tensile forces of bolts; $U_{wt,s}$: utilization of bolts due to elongation

$U_{t,s}$: utilization of bolts due to tension; $U_{vt,s}$: utilization of bolts due to shear; $U_{b,s}$: utilization of bolts due to bearing resistance

U_q : stress utilization of the beam; $U_{c/t}$: c/t-utilization of the beam; U_w : utilization of welds

U : total utilization

*) maximum utilization

2. final result

maximum utilization of end-plate due to 10 Lk: max U_p with corresponding values

node	x	y	u_z	b_z	m_{xx}	m_{yy}	m_{xy}	q_x	q_y	U_p
	mm	mm	mm	N/mm ²	kNm/m	kNm/m	kNm/m	kN/m	kN/m	
431	80.0	162.0	0.122	0.00	33.15	11.11	14.81	-2685.97	403.43	0.657

x,y: node coordinates; u_z : deformations (lifting off positive); b_z : compression by contact (compression positive); m_{xx}, m_{yy}, m_{xy} : moments
 q_x, q_y : shear forces; q_x, q_y : shear forces; U_p : utilization of end-plate

maximum utilization of bolts due to 10 Lk: max U_s with corresponding values

	x	y	F_t	U_{wt}	U_{vt}	U_b	U_s
	mm	mm	kN				
1	25.0	45.0	19.18	0.061	0.463	0.004	0.463
2	135.0	25.0	29.95	0.096	0.741	0.010	0.741
3	25.0	100.0	5.96	0.019	0.415	0.023	0.415
4	135.0	80.0	31.74	0.161	0.725	0.004	0.725
5	25.0	155.0	4.16	0.013	0.550	0.046	0.550
6	135.0	135.0	31.74	0.294	0.727	0.004	0.727

x,y: bolt coordinates; F_t : bolt force; U_{wt} : utilization due to elongation; U_{vt} : utilization due to shear

U_b : utilization due to bearing resistance; U_s : utilization of bolts

maximum utilization of end-plate [Lk 4]

maximum utilization of bolts due to elongation [Lk 4]

maximum utilization of bolts [Lk 4]

maximum utilization of the beam [Lk 8]

maximum utilization of welds [Lk 4]

maximum utilization [Lk 8]

max $U_p = 0.657 < 1$ ok

max $U_{wt,s} = 0.294 < 1$ ok

max $U_s = 0.856 < 1$ ok

max $(U_q, U_{ct}) = 0.916 < 1$ ok

max $U_w = 0.874 < 1$ ok

max $U = 0.916 < 1$ ok

verification succeeded

3. Regulations

EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;

Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010

EN 1990/NA, Nationaler Anhang zur EN 1990, Ausgabe Dezember 2010

EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;

Deutsche Fassung EN 1993-1-1:2005 + AC:2009, Ausgabe Dezember 2010

EN 1993-1-1/A1, Ergänzungen zur EN 1993-1-1, Ausgabe Juli 2014

EN 1993-1-1/NA, Nationaler Anhang zur EN 1993-1-1, Ausgabe Dezember 2018

EN 1993-1-8, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-8: Bemessung von Anschlüssen;

Deutsche Fassung EN 1993-1-8:2005 + AC:2009, Ausgabe Dezember 2010

EN 1993-1-8/NA, Nationaler Anhang zur EN 1993-1-8, Ausgabe Dezember 2010

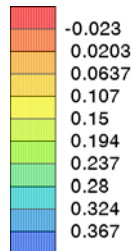
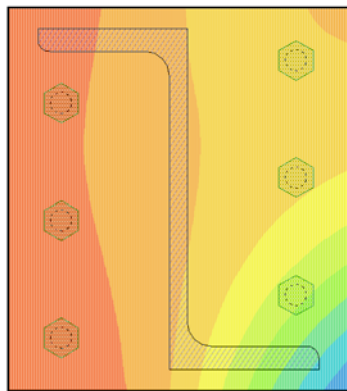
4. Lk 8 (decisive)

4.1. end-plate

design values: $N = 1.88 \text{ kN}$, $M_y = 2.08 \text{ kNm}$, $M_z = 11.15 \text{ kNm}$

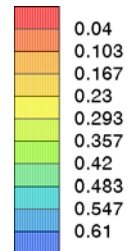
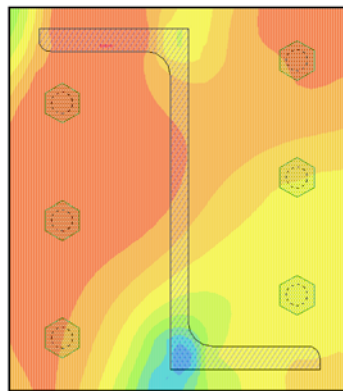
deformations u_z [mm]

min $u_z = -0.0234 \text{ mm}$, max $u_z = 0.3640 \text{ mm}$



utilization of end-plate U_p

min $U_p = 0.039$, max $U_p = 0.607$



deformations lifting off positive

utilization of end-plate

node	x mm	y mm	u_z mm	U_p
431	80.0	162.0	0.069	0.607
837	160.0	180.0	0.364	0.200

x,y: node coordinates; u_z : deformations (lifting off positive); U_p : utilization of end-plate

utilization of bolts

	x mm	y mm	w _t mm	F _t kN	ϵ_{wt} %	U_{wt}
1	25.0	45.0	0.010	3.39	0.032	0.011
2	135.0	25.0	0.068	23.60	0.226	0.075
3	25.0	100.0	0.010	3.43	0.033	0.011
4	135.0	80.0	0.095	31.40	0.315	0.105
5	25.0	155.0	0.002	0.76	0.007	0.002
6	135.0	135.0	0.179	31.74	0.598	0.199

x,y: bolt coordinates; w_t : deformation (tension positive); F_t : bolt force; ϵ_{wt} : elongation
 U_{wt} : utilization due to elongation

utilization of end-plate [node 431] $U_{max} = 0.607 < 1$ ok

utilization of bolts due to elongation [bolt 6] $U_{s,max} = 0.199 < 1$ ok

minimum plastic utilization of bolts $U_{pl,s,min} = 0.781 < 1$ ok

plastic utilization of tensile forces of bolts $U_{pl,t,s} = 0.708 < 1$ ok

4.2. bolts

design values: min $F_t = 0.76 \text{ kN}$, max $F_t = 31.74 \text{ kN}$, $V_z = 23.32 \text{ kN}$, $V_y = 5.55 \text{ kN}$,
 $M_x = 1.18 \text{ kNm}$

verification of bolts

U_{tp} utilization due to punching shear failure, U_{vt} utilization due to shear in tension, U_b utilization due to bearing resistance, U utilization of bolts

bolt 1	$U_{tp,1} = 0.009$	$U_{vt,1} = 0.401$	$U_{b,1} = 0.026$	$U_1 = 0.401$
bolt 2	$U_{tp,2} = 0.061$	$U_{vt,2} = 0.586$	$U_{b,2} = 0.008$	$U_2 = 0.586$
bolt 3	$U_{tp,3} = 0.009$	$U_{vt,3} = 0.388$	$U_{b,3} = 0.024$	$U_3 = 0.388$
bolt 4	$U_{tp,4} = 0.082$	$U_{vt,4} = 0.686$	$U_{b,4} = 0.001$	$U_4 = 0.686$
bolt 5	$U_{tp,5} = 0.002$	$U_{vt,5} = 0.352$	$U_{b,5} = 0.034$	$U_5 = 0.352$
bolt 6	$U_{tp,6} = 0.082$	$U_{vt,6} = 0.690$	$U_{b,6} = 0.000$	$U_6 = 0.690$
total:	$U_{tp} = 0.082$	$U_{vt} = 0.690$	$U_b = 0.034$	$U = 0.690 < 1$ ok

in utilization of bolts max U_s the minimum plastic utilization of bolts min $U_{pl,s} = 0.781$
and plastic utilization of tensile forces of bolts $U_{pl,t,s} = 0.708$ is included.

utilization of bolts $U_{max} = 0.781 < 1$ ok

4.3. beam

plastic verification for $N = 1.88 \text{ kN}$, $M_y = 2.08 \text{ kNm}$, $V_z = 23.32 \text{ kN}$, $M_z = 11.15 \text{ kNm}$

$V_y = 5.55 \text{ kN}$, $T_t = 1.18 \text{ kNm}$

internal forces and moments reg. yz-direction in kN, m: $M_y = 2.08$, $M_z = 11.15$, $V_y = 5.55$, $V_z = 23.32$

partial internal forces and moments of lines of cross-section in kN, m:

1: $N = -108.54$, $M_y = 0.00$, $M_z = 2.06$, $V_y = 2.77$, $V_z = 0.00$, $T = 0.39$

2: $N = 0.50$, $M_y = -14.20$, $M_z = 0.00$, $V_y = 0.00$, $V_z = 23.32$, $T = 0.41$

3: $N = 109.92$, $M_y = -0.00$, $M_z = 2.05$, $V_y = 2.77$, $V_z = 0.00$, $T = 0.39$

utilizations of lines of cross-section

1: $U_\sigma = 0.728$, $U_\tau = 0.518$, $U = 0.894$

2: $U_\sigma = 0.828$, $U_\tau = 0.390$, $U = 0.916$

3: $U_\sigma = 0.731$, $U_\tau = 0.518$, $U = 0.896$

max. load factor (plastic): $f_{pl} = 1.092$

utilization: $U_{pl} = 0.916$

verification: $U_{pl} = 0.916 < 1$ ok

c/t-verification: utilization $U_{c/t} = 0.473 < 1$ ok

utilization of the beam $\max(U_\sigma, U_{c/t}) = 0.916 < 1$ ok

4.4. welds

design values: $N = 1.88 \text{ kN}$, $M_y = 2.08 \text{ kNm}$, $V_z = 23.32 \text{ kN}$, $M_z = 11.15 \text{ kNm}$,

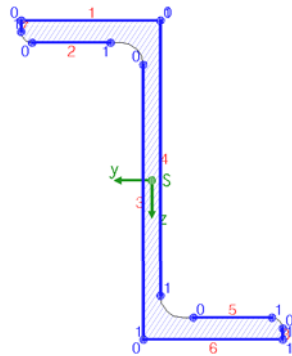
$V_y = 5.55 \text{ kN}$, $M_x = 1.18 \text{ kNm}$

weld 1: weld thickness $a = 10.0 \text{ mm} > a_{\max} = 0.7 \cdot t_{\min} = 7.7 \text{ mm}$ (welding technology, s. DIN 18800) !!

weld 3: weld thickness $a = 10.0 \text{ mm} > a_{\max} = 0.7 \cdot t_{\min} = 5.9 \text{ mm}$ (welding technology, s. DIN 18800) !!

weld 4: weld thickness $a = 10.0 \text{ mm} > a_{\max} = 0.7 \cdot t_{\min} = 5.9 \text{ mm}$ (welding technology, s. DIN 18800) !!

weld 6: weld thickness $a = 10.0 \text{ mm} > a_{\max} = 0.7 \cdot t_{\min} = 7.7 \text{ mm}$ (welding technology, s. DIN 18800) !!



weld 1: $a_w = 10.0 \text{ mm}$ $l_w = 70.0 \text{ mm}$

weld 2: $a_w = 10.0 \text{ mm}$ $l_w = 39.5 \text{ mm}$

weld 3: $a_w = 10.0 \text{ mm}$ $l_w = 138.0 \text{ mm}$

weld 4: $a_w = 10.0 \text{ mm}$ $l_w = 138.0 \text{ mm}$

weld 5: $a_w = 10.0 \text{ mm}$ $l_w = 39.5 \text{ mm}$

weld 6: $a_w = 10.0 \text{ mm}$ $l_w = 70.0 \text{ mm}$

weld 7: $a_w = 10.0 \text{ mm}$ $l_w = 5.5 \text{ mm}$

weld 8: $a_w = 10.0 \text{ mm}$ $l_w = 5.5 \text{ mm}$

Max: $\sigma_{1,w,Ed} = 351.39 \text{ N/mm}^2 < f_{1w,d} = 435.56 \text{ N/mm}^2$,

$\sigma_{2,w,Ed} = 175.70 \text{ N/mm}^2 < f_{2w,d} = 352.80 \text{ N/mm}^2 \Rightarrow U_w = 0.807 < 1$ ok

utilization of welds $U_{\max} = 0.807 < 1$ ok

4.5. total

utilization Lk 8 $U_{\max} = 0.916 < 1$ ok